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QP – 232

I Semester B.A./B.Sc. Examination, April/May 2021 (CBCS) (2020 – 21 and Onwards) (Fresh) Paper – I : MATHEMATICS

21

Time : 3 Hours

Max. Marks: 70

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(5×2=10)

Instruction : Answer all questions.

PART – A

- I. Answer any five questions.
 - a) Reduce the matrix $A = \begin{vmatrix} 1 & 3 & -2 \\ 2 & -1 & 4 \\ 1 & -11 & 14 \end{vmatrix}$ to echelon form.
 - b) Find the eigen values of the matrix $\begin{bmatrix} 5 & 4 \end{bmatrix}$
 - c) Find the nth derivative of sin²x.
 - d) If $z = x^3 4x^2y + 5y^2$, find $\frac{\partial^2 z}{\partial x \partial y}$
 - e) Evaluate $\int_{0}^{\pi/2} \cos^8 x \, dx$.
 - f) Evaluate $\int_{1}^{\pi/2} \sin^4 x \cos^2 x \, dx$.
 - g) Find the equation of the sphere whose centre is (3, -1, 4) and which passes through the point (1, -2, 0).
 - h) Show that the spheres $x^2 + y^2 + z^2 + 6y + 14z + 28 = 0$ and $x^2 + y^2 + z^2 + 6x + 8y + 4z + 24 = 0$ cut orthogonally.

PART – B

- II. Answer any three questions.
 - a) Find the rank of the matrix $A = \begin{bmatrix} 1 & 1 & -1 \\ 2 & -3 & 4 \\ 3 & -2 & 3 \end{bmatrix}$ by reducing it to normal form.

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 $(5 \times 3 = 15)$

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b) Solve the system of equations :

 $\begin{aligned} x_1 + 3x_2 + 2x_3 &= 0\\ 2x_1 - x_2 + 3x_3 &= 0\\ 3x_1 - 5x_2 + 4x_3 &= 0\\ x_1 + 17x_2 + 4x_3 &= 0. \end{aligned}$

- c) Show that the equations x + y + z = 6, x + 2y + 3z = 14, x + 4y + 7z = 30 are consistent and solve them.
- d) Find the eigen values and eigen vectors of the matrix $A = \begin{bmatrix} 5 & -1 \\ 4 & 9 \end{bmatrix}$.
- e) Using Cayley Hamilton theorem, find the inverse of the matrix $A = \begin{bmatrix} 0 & 2 & 1 \end{bmatrix}$

PART – C

(5×3=15)

 $(5 \times 2 = 10)$

- III. Answer any three questions.
 - a) Find the nth derivative of $\frac{x+3}{(x-1)(x+2)}$.
 - b) If x= sint and y = cospt then prove that $(1 x^2) y_{n+2} (2n+1)xy_{n+1} (n^2 p^2) y_n = 0.$
 - c) State and prove Euler's theorem for homogeneous function of two variables.
 - d) If $z = sin\left(\frac{x}{y}\right)$ and $x^2 + y^2 = a^2$, find $\frac{dz}{dx}$.
 - e) If $u = x^2 + y^2 + z^2$, v = xy + yz + zx, w = x + y + z. Find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. PART – D
- IV. Answer any two questions.
 - a) Obtain the reduction formula for $\int \sec^n x \, dx$, where n is a positive integer.
 - b) Evaluate $\int_{-\infty}^{\pi} x \sin^6 x \, dx$.
 - c) Evaluate $\int_{0}^{1} \frac{x^{a} 1}{\log x} dx$, where a is a parameter, using differentiation under integral sign.

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 $(5 \times 2 = 10)$

PART – E

- V. Answer any two questions.
 - a) Find the equation of the tangent plane to the sphere, $3(x^2 + y^2 + z^2) 2x 3y 4z 22 = 0$ at (1, 2, 3).

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- b) Find the equation of the right circular cone generated by revolving the line $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$ about the line $\frac{x}{-1} = \frac{y}{1} = \frac{z}{2}$.
- c) Find the equation of a right circular cylinder of radius 2 whose axis passes through (1, 2, 3) and has the direction cosines proportional to 2, -3, 6.

VI. Answer any two questions.

(5×2=10)

- a) If $y = (t^2 + 1)^2$ is the displacement of a particle. Find its velocity and acceleration at t = 2.
- b) If 15 kgs of commodity A and 17 kgs of commodity B together cost Rs. 241 and 25 kgs of commodity A and 13 kgs of commodity B together costs Rs. 279. Find the price of each per kg by using row reduced echelon form.
- c) If a metallic ball of radius 3 units is enclosed within a cylindrical pipe. Find the equation of the cylinder, if its axis is $\frac{x-1}{2} = \frac{y-2}{1} = \frac{z-3}{2}$.

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