



ED-322

M.Sc. 1st Semester
Examination, March-April 2021

COMPUTER SCIENCE

Paper - I

Mathematical Foundation of
Computer Science

Time : Three Hours] [Maximum Marks : 100

Note : Answer any **two** parts from each question. All questions carry equal marks.

Unit-I

1. (a) Prove that :

(i) $\sim(p \vee q) \Leftrightarrow (\sim p) \wedge (\sim q)$

(ii) $\sim(p \wedge q) \Leftrightarrow (\sim p) \vee (\sim q)$

(b) Explain the following terms and also give example to explain them :

(i) Quantifier

(ii) Negation of a Quantifier

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(2)

- (c) Let T be the set of all triangles in a plane and $R = \{(a, b) \mid \text{area of } \Delta a = \text{area of } \Delta b\}$; that is $a R b$ if and only if area of $\Delta a = \text{area of } \Delta b$. Prove that R is an equivalence relation.

Unit-II

2. (a) A lattice L is distributive if and only if $(a \vee b) \wedge (b \vee c) \wedge (c \vee a) = (a \wedge b) \vee (b \wedge c) \vee (c \wedge a)$
 $\forall a, b, c, \in L$.
- (b) Let (L, \vee, \wedge) be an algebraic system, where \vee and \wedge are binary operations satisfying the absorption law. Show that \vee and \wedge also satisfy the idempotent law.
- (c) If $(B, +, \cdot, ')$ is a Boolean algebra, then prove that the following statements are equivalent :
- (i) $a \cdot b' = 0$
- (ii) $a + b = b$
- (iii) $a' + b = 1$
- (iv) $a \cdot b = a$

Unit-III

3. (a) Prove that the inverse of the product of two elements of a group is the product of the inverse taken in the reverse order
i.e. $(ab)^{-1} = b^{-1} a^{-1} \forall a, b \in G$.

(3)

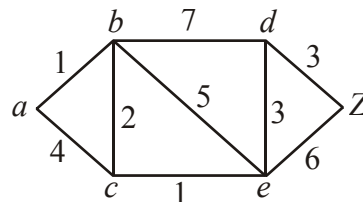
- (b) Define Grammar. Find the phase-structure grammar that generate the set :

$$L = \{a^n b^{2n}, n \geq 1\}$$

- (c) Show that the order of a subgroup of a finite group divides the order of the group.

Unit-IV

4. (a) Prove that in any graph, the number of vertices of odd degree is always even.
- (b) Prove that if the intersection of two path in a graph is a disconnected graph. Show that the union of the two path has at least one circuit.
- (c) Write an algorithm for shortest path in weighted graph and use it to find shortest path from a to z in the graph shown in figure where number associated with the edges are the weights.



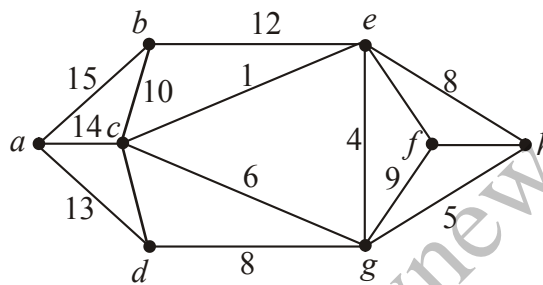
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(4)

Unit-V

5. (a) Find the minimum spanning tree for the graph :



- (b) Prove that A tree with n vertices has $(n - 1)$ edges.
- (c) Express the following algebraic expression in binary tree :
- (i) $(x - y) + ((y + z) + w)$
- (ii) $((a \times b) + c) - d \times (e + f)$