Roll No.

ED-2871

B. C. A. (Part III) EXAMINATION, 2021

Paper First

CALCULUS AND GEOMETRY

Time: Three Hours

Maximum Marks: 50

Note: All questions are compulsory. Attempt any two parts from each question. All questions carry equal marks.

- State and prove fundamental theorem of integral 1. (a) calculus.
 - (b) Let $f(x) = x^3$ on [0, 2], 2 > 0. Show that if $f \in \mathbb{R}[0, 2]$ and $\int_0^2 x^3 dx = \frac{2^4}{4}$
 - (c) Prove that if f is montonge on [a, b] and let 2 be continuous and increasing on [a, b]. Then $f \in R(2)$

Unit—II

2. (a) Discuss the maximum values of u in

$$u = xy + \frac{a^3}{x} + \frac{a^3}{y}$$

Find the maximum value of $x^2 + y^2 + z^2$ having (b) given:

$$ax + by + cz = p$$

(c) Find maximum and minimum value of $u = \sin x \sin y (x + y)$

Unit—III

- 3. (a) Show that $\int_{0}^{\infty} \sin x^2 dx$ is convergent.
 - (b) Test for convergence of $\int_0^1 x^{n-1} \log x \, dx$.
 - Test for convergence of $\int_0^1 x^{n-1} e^{-x} dx$ if o < n < 1Unit—IV

- Find the equation of the came whose vertex is (a) (1, 2, 3) and base curve is the $x^2 + y^2 + z^2 = 4$, x + y + z = 1circle
 - Find the angle between the lines of section of the plane 3x + y + 5z = 0and the came 6yz - 2zx + 5xy = 0
 - (c) Find the equation of the right circular cylinder whose radius is 2 and axis is the line

$$\frac{x-1}{2} = \frac{y}{3} = \frac{z-3}{3}$$

Unit-V

5. (a) If PSP' is the focal chord of a conic $\frac{l}{r} = 1 + ec \rightarrow o$ whose focus is S, then show that:

$$\frac{1}{SP} + \frac{1}{SP1} = \frac{2}{l}$$

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(b) Find the equation of the normal at a point ' α ' on the conic.

$$\frac{l}{r} = 1 + e\cos\theta$$

(c) If the tangoues at any point of an ellipse makes an angle α with its major axis and an angle β with the focal radius to the point of contact, then show that.

focal radius to the point of contact, then show that.
$$e\cos\alpha = \cos\beta$$