

ED-616

M.A./M.Sc. 3rd Semester Examination, March-April 2021 WS.II

MATHEMATICS

Optional (C)

Paper - III

Fuzzy Sets and its Applications - I

Time : Three Hours] [Maximum Marks: 80 Minimum Pass Marks : 16

Note : Answer any two parts from each question. All questions carry equal marks.

(a) Let $A_i \in F(x)$ for all $i \in I$, where I is an 1. index set. Then prove that

$$\bigcup_{i \in I}^{\alpha -} A_i \leq \left(\bigcup_{i \in I} A_i\right)$$

(b) State and prove second decomposition theorem.

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(Turn Over)

(2)

- (c) Prove that the standard Fuzzy intersection is the only idempotent *t*-norm.
- 2. (a) Prove that a *t*-norm *i* and an involute fuzzy complement *C*, the binary operation *u* on [0, 1] defined by u(a, b) = c (*i*(*a*), c(b)) for all $a, b \in [0, 1]$ is a *t*-conorm such that $\langle i, u, c \rangle$ is a dual triple.
 - (b) Let A and B are Fuzzy numbers with triangular shape in a Fuzzy equation as

$$A = \begin{cases} 0 & \text{for } x \le 3, x > 5 \\ x - 3 & \text{for } 3 < x \le 4 \\ 5 - x & \text{for } 4 < x \le 5 \end{cases}$$

$$B = \begin{cases} 0 & \text{for } x \le 12, x > 32\\ (x-12)/8 & \text{for } 12 < x \le 20\\ (32-x)/12 & \text{for } 20 < x \le 32 \end{cases}$$

Find the solution of equation $A \cdot X = B$.

- (c) Prove that that < i, u, c > be a dual triple. Then prove that the Fuzzy operations i, u, c satisfy the law of excluded middle and the law of contradiction.
- **3.** (a) Prove that for Fuzzy sets

MIN [A, MAX (A B)] = A.

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(Continued)

(3)

(b) Let R be a reflexible Fuzzy relation on X^2 , where $|X| = n \ge 2$. Then prove that

$$R_{T(i)} = R^{(n-1)}$$

(c) Solve the following Fuzzy relation equation using max-min composition

$$P \circ \begin{bmatrix} .9 & .6 & 1 \\ .8 & .8 & .5 \\ .6 & .4 & .6 \end{bmatrix} = \begin{bmatrix} .6 & .6 & .5 \end{bmatrix}$$

- 4. (a) If R symmetric, then prove that each power of R is symmetric.
 - (b) Explain Fuzzy compatibility relations.
 - (c) Explain Fuzzy graphs.
- 5. (a) Prove that every possibility measure 'Pos' on a finite power set P(x) is uniquely determined by a possibility distributive function $r: X \to [0, 1]$ via the formula. pos $(A) = \max r(x)$ for each $A \in P(X)$.
 - (b) Explain the Evidence theory.
 - (c) Let a given finite body of evidence (ε . *m*) be nested, then prove that for all $A, B \in P(X)$, we have
 - (i) $\operatorname{bel}(A \cap B) = \min[\operatorname{bel}(A), \operatorname{bel}(B)]$
 - (*ii*) $Pl(A \cup B) = \max[Pl(A), Pl(B)]$

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