



ED-616

M.A./M.Sc. 3rd Semester
Examination, March-April 2021

MATHEMATICS

Optional (C)

Paper - III

Fuzzy Sets and its Applications - I

Time : Three Hours] [Maximum Marks : 80
[Minimum Pass Marks : 16

Note : Answer any **two** parts from each question. All questions carry equal marks.

1. (a) Let $A_i \in F(x)$ for all $i \in I$, where I is an index set. Then prove that

$$\bigcup_{i \in I} \alpha^{-} A_i \leq \left(\bigcup_{i \in I} A_i \right)^{\alpha}$$

- (b) State and prove second decomposition theorem.

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(Turn Over)

(2)

- (c) Prove that the standard Fuzzy intersection is the only idempotent t -norm.
2. (a) Prove that a t -norm i and an involute fuzzy complement C , the binary operation u on $[0, 1]$ defined by $u(a, b) = c(i(a), c(b))$ for all $a, b \in [0, 1]$ is a t -conorm such that $\langle i, u, c \rangle$ is a dual triple.
- (b) Let A and B are Fuzzy numbers with triangular shape in a Fuzzy equation as

$$A = \begin{cases} 0 & \text{for } x \leq 3, x > 5 \\ x - 3 & \text{for } 3 < x \leq 4 \\ 5 - x & \text{for } 4 < x \leq 5 \end{cases}$$

$$B = \begin{cases} 0 & \text{for } x \leq 12, x > 32 \\ (x - 12)/8 & \text{for } 12 < x \leq 20 \\ (32 - x)/12 & \text{for } 20 < x \leq 32 \end{cases}$$

Find the solution of equation $A \cdot X = B$.

- (c) Prove that that $\langle i, u, c \rangle$ be a dual triple. Then prove that the Fuzzy operations i, u, c satisfy the law of excluded middle and the law of contradiction.

3. (a) Prove that for Fuzzy sets

$$\text{MIN} [A, \text{MAX} (A B)] = A.$$

(3)

(b) Let R be a reflexible Fuzzy relation on X^2 , where $|X| = n \geq 2$. Then prove that

$$R_{T(i)} = R^{(n-1)}.$$

(c) Solve the following Fuzzy relation equation using max-min composition

$$P \circ \begin{bmatrix} .9 & .6 & 1 \\ .8 & .8 & .5 \\ .6 & .4 & .6 \end{bmatrix} = [.6 \quad .6 \quad .5]$$

4. (a) If R symmetric, then prove that each power of R is symmetric.

(b) Explain Fuzzy compatibility relations.

(c) Explain Fuzzy graphs.

5. (a) Prove that every possibility measure 'Pos' on a finite power set $P(X)$ is uniquely determined by a possibility distributive function $r: X \rightarrow [0, 1]$ via the formula. $\text{pos}(A) = \max r(x)$ for each $A \in P(X)$.

(b) Explain the Evidence theory.

(c) Let a given finite body of evidence (ϵ, m) be nested, then prove that for all $A, B \in P(X)$, we have

$$(i) \text{ bel}(A \cap B) = \min[\text{bel}(A), \text{bel}(B)]$$

$$(ii) \text{ Pl}(A \cup B) = \max[\text{Pl}(A), \text{Pl}(B)]$$